# Задача A. Milkshakes

Имя входного файла: Имя выхолного файла: Ограничение по времени: Ограничение по памяти:

milkshakes.in milkshakes.out 1 second 64 MB

You own a milkshake shop. There are N different flavors that you can prepare, and each flavor can be prepared malted or unmalted. So, you can make 2N different types of milkshakes.

Each of your customers has a set of milkshake types that they like, and they will be satisfied if you have at least one of those types prepared. At most one of the types a customer likes will be a malted flavor.

You want to make N batches of milkshakes, so that:

- There is exactly one batch for each flavor of milkshake, and it is either malted or unmalted.
- For each customer, you make at least one milkshake type that they like.
- The minimum possible number of batches are malted.

Find whether it is possible to satisfy all your customers given these constraints, and if it is, what milkshake types you should make.

If it is possible to satisfy all your customers, there will be only one answer which minimizes the number of malted batches.

### Формат входного файла

• One line containing an integer C, the number of test cases in the input file.

For each test case, there will be:

- One line containing the integer N, the number of milkshake flavors.
- One line containing the integer M, the number of customers.
- *M* lines, one for each customer, each containing:
  - An integer  $T \ge 1$ , the number of milkshake types the customer likes, followed by
  - -T pairs of integers XY, one for each type the customer likes, where X is the milkshake flavor between 1 and N inclusive, and Y is either 0 to indicate unmalted, or 1 to indicated malted. Note that:

- \* No pair will occur more than once for a single customer.
- \* Each customer will have at least one flavor that they like  $(T \ge 1)$ .
- \* Each customer will like at most one malted flavor. (At most one pair for each customer has Y = 1).

All of these numbers are separated by single spaces.

 $C \le 100$  $1 \le N \le 2000$  $1 \le M \le 2\,000$ 

 $\sum_{k=1}^{k=C} M \leqslant 10\,000$ 

The sum of all the T values for the customers in a test case will not exceed 3000.

### Формат выходного файла

- C lines, one for each test case in the order they occur in the input file, each containing the string "Case #X: "where X is the number of the test case, starting from 1, followed by:
  - The string IMPOSSIBLE, if the customers' preferences cannot be satisfied; OR.
  - -N space-separated integers, one for each flavor from 1 to N, which are 0 if the corresponding flavor should be prepared unmalted, and 1 if it should be malted.

#### Пример

milkshakes.in	milkshakes.out
2	Case #1: 1 0 0 0 0
5	Case #2: IMPOSSIBLE
3	
1 1 1	
2 1 0 2 0	
150	
1	
2	
1 1 0	
1 1 1	

### Задача В. Plus minus

Имя входного файла:	plusminus.in
Имя выходного файла:	plusminus.out
Ограничение по времени:	$1  \mathrm{second}$
Ограничение по памяти:	$64 \mathrm{MB}$

В каждой клетке поля  $M \times N$  стоит либо плюс, либо минус. За один ход разрешается поменять знаки на противоположные в любом квадрате  $2 \times 2$ . Можно ли с помощью таких операций получить во всех клетках поля знаки плюс?

#### Формат входного файла

В первой строке числа M <br/>иN (1  $\leqslant$   $N,M\leqslant$  1000). В следующих<br/> N строках содержится по M символов +, либо -.

#### Формат выходного файла

Ответ на вопрос задачи: слово Yes или No

#### Пример

plusminus.in	plusminus.out
3 3	No
_+_	
_+_	
++-	
3 3	Yes
_+_	
+++	
_+_	

# Задача С. Про спрайт

Имя входного файла:	sprite.in
Имя выходного файла:	sprite.out
Ограничение по времени:	$1  \mathrm{second}$
Ограничение по памяти:	$64 \mathrm{MB}$

86 класс решил на слет взять много Спрайта. Для этого они собрались сконструировать переносной холодильник  $a \times b \times c$ , который будет вмещать ровно n кубических банок Спрайта размером  $1 \times 1 \times 1$  Чтобы лимонад доехал как можно более холодным, они хотят минимизоровать теплопотери; то есть минимизировать площадь поверхности.

Например, если емкость холодильника должна равняться 12, то возможны следующие варианты:

	$322 \rightarrow 32$
	$431 \rightarrow 38$
	$621 \rightarrow 40$
	$1211 \rightarrow 50$
	В этом примере оптимальным является холодильник 322.
_	Помогите 8б найти оптимальный холодильник в общем случае.

Формат входного файла

Число  $n \ (1 \le n \le 10^6)$ 

#### Формат выходного файла

Три числа a, b, c  $(1 \le n \le 10^6)$  — размеры наилучшего холодильника. Числа нужно выводить в порядке неубывания.

#### Пример

sprite.in	sprite.out
12	2 2 3
13	1 1 13
100000	100 100 100

# Задача D. Уникальное число

unique.in
unique.out
1 second
$64 \mathrm{MB}$

Дано нечетное количество чисел, из которых все кроме одного разбиваются на пары одинаковых. Найдите единственное число без пары.

### Формат входного файла

Число  $n \ (1 \le n \le 10^5)$ . Далее n целых чисел, по модулю не превосходящие  $10^{18}$ .

#### Формат выходного файла

Число без пары.

### Пример

unique.in	unique.out
7	566
239 566 470 30 30 239 470	
1	-30
-30	

# Задача E. Strange Digits

Имя входного файла:	digits.in
Имя выходного файла:	digits.out
Ограничение по времени:	$2  {\rm seconds}$
Ограничение по памяти:	256 megabyte

In decimal notation we use digits from 0 to 9. If we didn't use some digit, we wouldn't be able to write down some numbers, for example, if we didn't use digit 1, there would be no way to write down number 10. On the other side, if we used more digits than necessary, for example, digit A (with weight equal to 10), there would be several ways to write down the same number. For example, the number 110 could also be written as AA. Similar argument can be applied to notation with any base b.

Consider a notation with base b and digits  $c_1, c_2, \ldots, c_k$  chosen from the set  $\{0, 1, \ldots, 9, A, B, \ldots, Z\}$  (the weights of digits 0 through 9 are equal to their ordinary weights, the weight of A is 10, the weight of B is 11, etc, the weight of Z is 35). You are given a number n. Find out whether you can write it down in the notation with base b using only given digits, and whether there is a unique way to do so.

#### Формат входного файла

The first line of the input file contains b ( $2 \le b \le 36$ ). The second line of the input file contains  $c_1, c_2, \ldots, c_k$  in the increasing order without spaces ( $1 \le k \le 36, c_1 = 0$ ). The third line contains n ( $1 \le n \le 10^{100}$ ), it is presented in ordinary decimal notation.

### Формат выходного файла

If it is impossible to write down n in the described way, output "Impossible" at the first line of the output file.

If there is a unique way to write down n in the described way, output "Unique" at the first line of the output file. In this case print the presentation of n in the described notation at the second line.

If there are several ways to write down n in the described way, output "Ambiguous" at the first line of the output file. Print any presentation of n in the described notation at the second line.

#### Примеры

digits.in	digits.out
10	Ambiguous
0123456789A	AA
110	
10	Impossible
023456789	
10	
10	Unique
023456789A	A
10	

# Задача F. Fire Station Building

Имя входного файла:	fire.in
Имя выходного файла:	fire.out
Ограничение по времени:	2 seconds
Ограничение по памяти:	256 Mebibytes

There is a country with N cities connected by M bidirectional roads, and you need to build a fire station somewhere. Of course, your problem would be too simple without the following restrictions:

- Firemen should be able to reach any city from fire station by roads only.
- You want to minimize expected distance from fire station to place of fire. For this purpose, probability of a fire is given to you for every city. Assume that firemen always choose the shortest way to fire.
- You can place fire station not only in cities but on the roads between them as well. Moreover, sanity regulations of the country forbid placement of a fire station closer than at a distance R from cities. Distances are measured on roads only, so you can place fire station on a road if its length is not less than 2R, and you should not worry about distances to cities not adjacent to the given road. In particular, R = 0 means that you are allowed to place a fire station in cities.



Example of a country with three cities and three roads. Places where you can build fire station are marked with bold line and bold dot.

You are given a complete description of the country. Find the best place for a fire station in it.

#### Формат входного файла

The first line of input file contains integer numbers N, M and R  $(1 \le N \le 100, 0 \le M \le N(N-1)/2, 0 \le R \le 10^4)$ . Second line contains N integer numbers — probabilities of a fire in each city. Numbers are non-negative integers given in hundredths of percent (that is, sum to  $10^4$ ). Each of the next M lines contains description of one road, namely three integer numbers  $A_i$ ,  $B_i$  and  $L_i$  — endpoints of the road and its length in kilometers  $(1 \le A_i < B_i \le N, 1 \le L_i \le 10^4)$ . There can be at most one road between any two cities.

#### Формат выходного файла

Output only one number — expected length of a way to fire in kilometers assuming fire station is built optimally. This number should be precise up to 1 meter. If by some

reason it is impossible to build fire station that fulfills all the requirements, write to the output file number -1 instead.

Примеры

fire.in	fire.out
3 3 20	26.00000
3000 5000 2000	
1 2 40	
1 3 50	
2 3 30	
3 1 20	-1
3000 5000 2000	
1 3 50	

In the first example (which corresponds to the picture above) it is optimal to build fire station in the middle of the first road. In the second example it is impossible to build fire station satisfying all the requirements. In particular, any fire station on the map will violate requirement one (since the country is disconnected).